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Design of Room Temperature Electrically Pumped Visible Semiconductor Nanolasers

Yuanlong Fan and K. Alan Shore, *Senior Member, IEEE*

Abstract—This paper presents a comprehensive theoretical study of the optical and thermal properties of an electrically pumped semiconductor nanolaser (SNL) having an GaN/(InGaN/GaN MQWs)/GaN core shell structure. Numerical results show that the lasing whispering-gallery mode (WGM) has a threshold gain of 413 cm^{-1} . Furthermore, it is shown that when it is operated well-above threshold, the device temperature increases by only 22 K above an ambient temperature of 300 K. These promising results are attributed to the strong mode confinement in the active region and the good thermal properties of the material system of the proposed structure. The results presented in this paper offer guidelines for fabrication of electrically pumped room temperature continuous wave SNL operating in the visible spectral region.

Index Terms—semiconductor nanolasers, photonic integrated circuits, gallium nitride.

I. INTRODUCTION

DURING the last two decades, extensive research effort has been devoted to the design of semiconductor nanolasers (SNLs) whose size are generally of order the lasing wavelength or even subwavelength scale [1-3]. Apart from their ultra-small size, SNLs are also characterized by their low power consumption [4-6], potential for high modulation bandwidth [7-9] and good compatibility with existing technologies such as photonic integrated circuits and lab-on-a-chip [10-12].

Amongst various existing SNLs [13-30], the so-called metal coated SNL (MCSNL) [15, 17, 23, 25, 26, 31, 32] has gained much attention in recent years due to its ingenious structure. The MCSNL mainly consists of an axially double heterostructured p-i-n pillar, a thin insulating layer surrounding the pillar and metal encapsulating the insulating layer and the pillar. Such configuration has the following advantages:

- Ease of fabrication: the pillar can be formed using standard dry-etching techniques, followed by thin-film deposition and sputtering to introduce the insulating layer and metal respectively [3];
- The choice of two alternative modes: depending on the thickness of the insulating layer, either photonic or plasmonic modes can be supported;

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- The ease of electrical injection: the carriers can be injected through the top of the pillar via the coated metal and the base of the pillar via a large-area lateral contact. At the same time, the insulating layer prevents shorting of the diode junction;
- An ultra-small footprint (smaller than free-space laser wavelength λ_0) in all three dimensions due to the ability of the metal to tightly confine the mode to challenge the diffraction limit ($\lambda_0/2n$, where n is the refractive index).
- The elimination of optical interference between adjacent devices in photonic integrated circuits due to the coated metal [32].

The first MCSNL under electrical injection was experimentally demonstrated by Hill et al. in 2007 [15]. Continuous wave (CW) lasing at the wavelength of around $1.4 \mu\text{m}$ was observed with a cylindrical pillar of diameter 260 nm which almost reaches the diffraction limit. However, this device was operated at cryogenic temperature (77 K) due to the high optical loss in the metal at higher temperature. Since then, various attempts have been made to further decrease the size of the MCSNL and increase the operating temperature by compensating the loss introduced by the metal. For example, in 2011, an operating temperature of 140 K was achieved [23] using pillar undercut to improve the vertical mode confinement and subsequently lower the threshold gain. Theoretical work has also been undertaken to explore the possibility of room temperature (RT) operation for such undercut structures [32, 33]. Another method to reduce the metal loss is the use of a thick insulating layer between the active region and the metal to reduce the modal overlap with the metal [19, 34]. With these efforts, in 2012, RT CW electrical injection operation of MCSNL lasing at $1.55 \mu\text{m}$ was achieved [25] based on a rectangular pillar with a volume of only $0.42\lambda_0^3$.

After successfully demonstrating electrically pumped RT CW MCSNL operating in the near infrared spectral region, it is natural to consider if such a structure may also be utilized in the visible spectral range where demand for novel sources arises from various emerging technologies such as Li-Fi and ultra-high definition (UHD) displays. However, to date, there have been no reports of RT CW electrical pumped MCSNLs or indeed any other SNLs, e.g., surface plasmonic SNLs which currently can be operated under RT optical injection with extremely small cavity sizes [35-37], in the visible spectral range. One likely reason is the poor mode confinement caused by the small refractive index difference between relevant materials of the cladding and active region. For example, in a

near infrared MCSNL with $\lambda_0=1.55 \mu\text{m}$, the pillar of InP/InGaAs/InP has refractive indices of 3.1/3.4/3.1 [31] where the effective refractive index of InP can be further decreased by introducing undercut as mentioned above. However, in the visible MCSNL with $\lambda_0=465 \text{ nm}$, if the pillar is GaN/(InGaN/GaN MQWs)/GaN which is commonly used in existing visible SNLs [27, 29, 30, 38], the refractive indices are 2.42/2.45/2.42 [39]. This gives a refractive index difference of 0.03 which is ten times smaller than that of the near infrared MCSNL. Moreover, it is challenging to undercut GaN due to its intrinsic crystal structure.

Recently, a radially double heterostructured p-i-n pillar structure SNL [29], namely the core-shell SNL, was experimentally demonstrated to tackle the above-mentioned issue in the visible spectral range. The core of this structure is the n doped GaN which is surrounded by InGaN/GaN MQWs and then the outer shell which is p doped GaN. In such a structure, the volume of the active region is one or more orders of magnitude greater than that of the axially double heterostructured p-i-n pillar. Moreover, the quantum-confined stark effect (QCSE) in the MQWs is eliminated which leads to a higher quantum efficiency and spectral stability [29, 40]. Lower transparency carrier density and Auger coefficient were also reported [41, 42] which should assist to decrease the lasing threshold. Lasing at a wavelength of 391 nm was observed at RT but under pulsed optical pumping. To achieve electrical pumping without significant increase of temperature, one possible way is to coat the core-shell SNL with metal which is similar to that which has been done for near infrared MCSNLs.

The aim of this paper is to numerically investigate the possibility of lasing behaviour in the visible of electrically pumped RT CW MCSNL with a core-shell structure. Firstly, the numerical model for the core-shell MCSNL is introduced where its three main physical properties are considered, namely optical, electrical and thermal properties. Such a structure will be shown to have low losses. By combining with the electrical and thermal simulations, the possibility of lasing behaviour of the core-shell MCSNL is discussed. Finally, conclusions are drawn based on the results obtained.

II. NUMERICAL MODEL

A schematic illustration of the core-shell MCSNL and its cross-sectional-view are, respectively, shown in Fig. 1 (a) and (b). The core-shell MCSNL is situated on a GaN-on-Sapphire substrate where GaN is N doped and used as a contact layer connected to the electrical contact (N Contact). The core of the MCSNL is N GaN which is sequentially and uniformly coated by the shells of InGaN/GaN MQWs, P GaN, SiO₂ and silver respectively with a thickness of t_{MQW} , t_P , t_S and t_M . The SiO₂ prevents electrically shorting the diode. Silver is used to confine the mode and as a contact layer connecting to the P Contact. The fabrication process of the GaN/(InGaN/GaN MQWs)/GaN based core-shell structure can be found in [29, 30] and the method in [23] can be used to introduce the shells of SiO₂ and silver. The size of each layer is shown in Table I. It should be pointed out that fabricated devices may deviate from the ideal in, for example, having some side-wall tilt. In

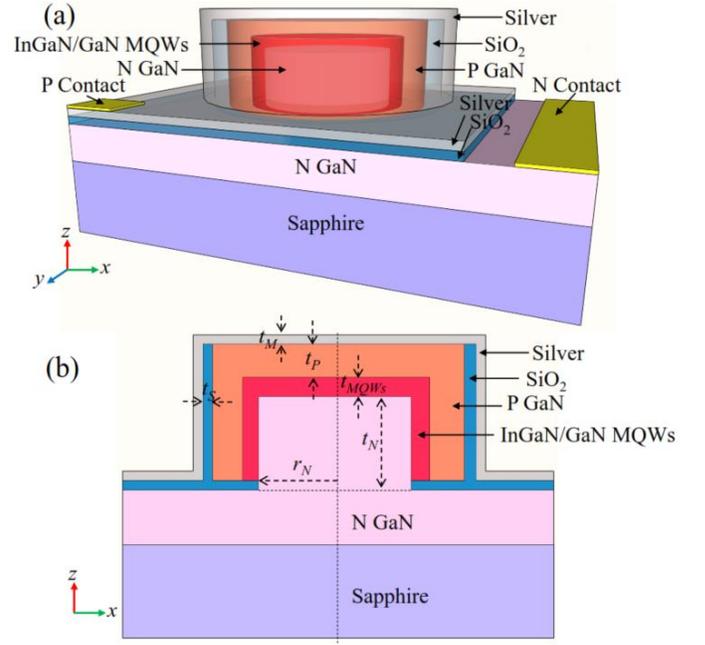


Fig. 1. The schematic illustration of the core-shell MCSNL. (a) 3D view. (b) cross-sectional-view.

addition, surface roughness may be introduced in the fabrication process. Such imperfections can degrade the performance of SNL [33, 43]. Therefore, the design of a robust SNL whose performance is substantially insensitive to such fabrication processes is desired. In the following section (Section III), it shows the proposed SNL has a low threshold gain which is more than four times lower than the available material gain calculated in [44], thus providing a significant immunity to defects introduced in the fabrication process.

TABLE I
THE SIZE OF EACH LAYER OF THE MCCSSNL

Layer Name	Material	Size
N Doped Core	N GaN	$r_N=200 \text{ nm}$, $t_N=425\text{-}625 \text{ nm}$
InGaN in MQWs	InGaN	2 nm
GaN in MQWs	GaN	10 nm
MQWs	InGaN/GaN	$t_{MQW}=8 \text{ pairs}$
P Doped Shell	P GaN	$t_P=35\text{-}75 \text{ nm}$
Insulating Shell	SiO ₂	$t_S=20\text{-}60 \text{ nm}$
Metal Shell	Ag	$t_M=40 \text{ nm}$

A commercial simulator (COMSOL Multiphysics) based on the finite element method (FEM) [45] is used to perform the numerical simulations of the core-shell MCSNL. In particular, three main physical properties of the core-shell MCSNL are investigated, namely optical, electrical and thermal properties which are respectively simulated using Optics, Semiconductor and Heat Transfer modules provided by the COMSOL. Details of the model in each module is described in the following sub-sections.

A. Model for Optical Simulations

In the model, the core-shell MCSNL is surrounded by the air which is then enclosed by perfect matched layers (PMLs) to ensure no back-reflections of the light. The maximum element size for the finite element analysis and refractive index of each

layer used in the simulations are listed in Table II. Note that the maximum element size should be limited to a fraction of the wavelength; the quicker the field is expected to change, the smaller the maximum element size which should be used.

TABLE II
MAXIMUM ELEMENT SIZE AND REFRACTIVE INDEX USED IN THE OPTICAL SIMULATIONS

Material	Maximum Element Size	Refractive Index ($\lambda_0=465$ nm)
N GaN	$\lambda_0/n_{\text{GaN}}/3$	$n_{\text{GaN}}=2.42$ [39]
InGaN/GaN MQWs	$\lambda_0/n_{\text{MQWs}}/4$	$n_{\text{MQWs}}=2.45$ [39]
P GaN	$\lambda_0/n_{\text{GaN}}/3$	$n_{\text{GaN}}=2.42$ [39]
SiO ₂	$\lambda_0/n_{\text{SiO}_2}/4$	$n_{\text{SiO}_2}=1.55$ [48]
Sapphire	$\lambda_0/n_{\text{Sapphire}}/4$	$n_{\text{Sapphire}}=1.78$ [49]
Ag	$\lambda_0/4$	$n_{\text{Ag}}=0.05-2.80i$ [50]
Air	$\lambda_0/4$	$n_{\text{Air}}=1$ [51]

Full 3D optical simulations are performed using the electromagnetic waves (frequency domain) interface in the Optics module which finds the eigenmodes for a given cavity by solving the wave equations. The PARDISO solver in the COMSOL is used to search for eigenmodes around a preset initial guess of the free-space resonance wavelength $\lambda_0=465$ nm which corresponds to the peak of the gain spectrum calculated in [44]. The number of returned eigenmodes is set to be 100 which gives the modes with free-space wavelengths within a 25-35 nm range of λ_0 , depending on the size of the laser. These eigenmodes includes both physical and spurious modes which can be distinguished by their spatial variations. The physical modes have spatial variations that are comparable to the cavity size whereas the spurious modes have spatial variations that are comparable to the mesh size [46]. After filtering out the spurious modes, the threshold gain is calculated and compared with the material gain calculated in [44] to examine the possibility of lasing in the proposed core-shell MCSNL. The threshold gain, g_{th} is calculated by [32, 47]:

$$g_{\text{th}} = \frac{2\pi n_g}{\lambda Q \Gamma} \quad (1)$$

where n_g is the group refractive index of the active region, λ is the resonance wavelength, Q is the quality factor and Γ is the confinement factor. λ and Q are calculated from the eigenfrequencies of the eigenmodes. Γ is the confinement factor which is calculated as the ratio of total electric energy density in the active region and in the whole core-shell MCSNL. From (1), it can be seen that the general rules for designing a SNL with a low threshold gain is to (i) to increase the Q factor which can be achieved by avoiding modal overlap with the metal and (ii) to maximize the mode confinement in the active region.

B. Model for Electrical and Thermal Simulations

The electrical and thermal simulations are performed together by coupling the Semiconductor interface in the Semiconductor module and the Heat Transfer in Solid interface in the Heat Transfer module. The Semiconductor interface solves Poisson's equation in conjunction with continuity equations for

the charge carriers considering Fermi-Dirac statistics. The Heat Transfer in Solid interface solves the heat balance equation in time.

Using an initial temperature, the heat generated in the Semiconductor interface, including joule and non-radiative recombination heating, due to electrical injection are used as the heat source in the Heat Transfer in Solid interface which calculates the temperature distribution. This temperature distribution is then fed back to the Semiconductor interface which re-calculates the heat source and again provides the heat source to the Heat Transfer in Solid interface to update the temperature distribution. This process iterates several times until the steady-state of the temperature distribution is reached.

In the model, 2D axial-symmetric geometry is used where the ambient temperature is set to be 300 K and the bottom of the Sapphire is set to a constant temperature of 300 K to act as a heat sink. The Metal Contact boundary condition is used to inject the carries into the laser where the holes are injected from top surface of the P GaN (p doped $1.0 \times 10^{19} \text{ cm}^{-3}$) shell and electrons are injected from the N GaN (n doped $1.0 \times 10^{19} \text{ cm}^{-3}$) layer sit on top of the sapphire substrate. The maximum element size in the active region is set to be 5 nm which is gradually increased and swept over the whole geometry. Several key physical processes, including radiative recombination, Auger recombination, trap-assisted recombination and convective heat flux via the metal, are considered in the simulations. Parameters used for electrical and thermal simulations are listed in Table III and IV.

TABLE III
PARAMETERS USED IN THE ELECTRICAL SIMULATIONS

Parameters	Material	GaN (InGaN)
Band gap		3.39 eV (2.67eV) [52]
Electron affinity		4.1 V [53]
Effective density of states (Valence band)		$(T/1 \text{ K})^{3/2} \times 8.9 \times 10^{15} \text{ cm}^{-3}$ [54]
Effective density of states (Conduction band)		$(T/1 \text{ K})^{3/2} \times 4.3 \times 10^{14} \text{ cm}^{-3}$ [54]
Electron mobility		$1000 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ [55]
Hole mobility		$200 \text{ cm}^2 \text{V}^{-1} \text{s}^{-1}$ [56]
Radiative recombination factor		$1.0 \times 10^{-11} \text{ cm}^3 \text{s}^{-1}$ [57]
Auger recombination factor		$6.15 \times 10^{-33} \text{ cm}^6 \text{s}^{-1}$ [42]
SRH recombination factor		$2.0 \times 10^{-7} \text{ s}$ [57]

*T is the temperature.

III. OPTICAL SIMULATION RESULTS

In this section, attention is given to a range of circumstances in which the core-shell MCSNLs are shown to have low losses where the carrier density is $6 \times 10^{19} \text{ cm}^{-3}$ and temperature is 300 K. This carrier density and temperature will be used as a reference for the electrical and thermal simulation results shown in the following sections. Figure 2 shows the influence of N GaN thickness on the threshold gain and Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_{MQW}=96$ nm, $t_P=80$ nm and $t_S=40$ nm. From Fig. 2, it can be seen that g_{th} decreases with the increase of t_N and Q increases with the increase of t_N . Also, with the increase of t_N , the wavelength is red-shifted which makes the material gain, g_0 , move towards its peak as shown in [44] where the wavelength is 465.60 nm.

TABLE IV
PARAMETERS USED IN THE THERMAL SIMULATIONS

Material	GaN (InGaN)	SiO2	Ag	Sapphire
Thermal conductivity	130 Wm ⁻¹ K ⁻¹ [58]	1.4 Wm ⁻¹ K ⁻¹ [59]	429 Wm ⁻¹ K ⁻¹ [60]	35 Wm ⁻¹ K ⁻¹ [61]
Density	6070 kgm ⁻³ [62]	2200 kgm ⁻³ [63]	10500 kgm ⁻³ [64]	3965 kgm ⁻³ [65]
Heat capacity at constant pressure	490 Jkg ⁻¹ K ⁻¹ [66]	730 Jkg ⁻¹ K ⁻¹ [67]	235 Jkg ⁻¹ K ⁻¹ [64]	880 Jkg ⁻¹ K ⁻¹ [65]

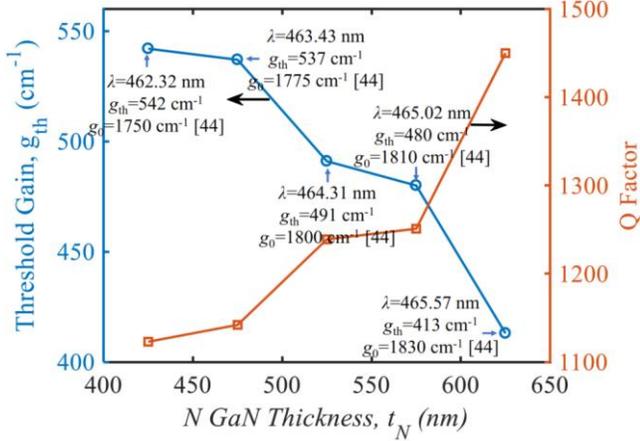


Fig. 2. The influence of N GaN thickness on the threshold gain and Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_{MQW}=96$ nm, $t_P=80$ nm and $t_S=40$ nm.

The modes are whispering-gallery modes (WGM_{m,n}) with the azimuthal mode number (m) of 6 and radial mode number (n) of 2. An example of the mode profile, in terms of electric field intensity, is shown in Fig. 3 when $t_N=625$ nm. The threshold gains shown in Fig. 2 are all lower than the material gain calculated in [44] and therefore lasing can be supported. In particular, when $t_N=625$ nm, g_{th} is only 413 cm⁻¹ which is much lower than the material gain ($g_0=1830$ cm⁻¹) calculated in [44]. The corresponding mode is shown in Fig. 3. It can be seen that this WGM is well confined in the core-shell MCSNL due to the metal coating. Most of the first order radial mode, which occupies the majority of the electric field intensity, is well confined in the active region with $\Gamma=55.2\%$. This Γ will decrease, e.g., $\Gamma=54.2\%$ when $t_N=475$ nm, with decrease of nanolaser height as parts of the mode leak into the substrate and the top P GaN where additional losses can also be introduced due to the metal coated on top of the P GaN. This is why g_{th} increases with decrease of t_N as shown in Fig. 2.

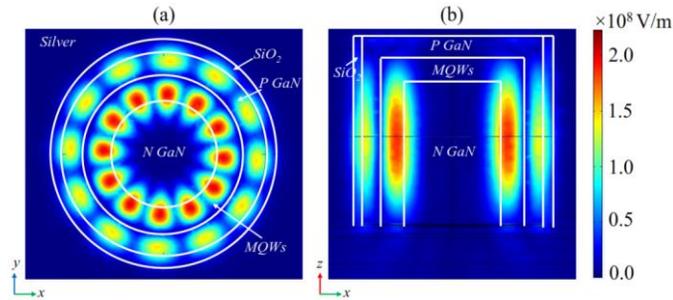


Fig. 3. The electric field amplitude intensity (WGM_{6,2}) in a core-shell MCSNL where $r_N=200$ nm, $t_N=625$ nm, $t_{MQW}=96$ nm, $t_P=80$ nm and $t_S=40$ nm. (a) horizontal cross section, (b) vertical cross section.

Attention is now given to the effect of the SiO₂ thickness on

the threshold gain and the Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_N=625$ nm, $t_{MQW}=96$ nm and $t_P=80$ nm. Figure 4 shows the effect of SiO₂ thickness where the threshold gain decreases with increase of t_S and the Q factor increases with the increase of t_S . This is because increase of the SiO₂ thickness increases the distance between the mode and metal thus reducing the losses. However, when the SiO₂ thickness is larger than 40 nm, the g_0 starts to decrease dramatically from 1830 cm⁻¹ ($t_S=40$ nm) to 190 cm⁻¹ ($t_S=60$ nm) where the wavelength red-shifts from 465.57 nm to 473.13 nm according to the gain spectrum in [44]. Such a rapid drop of material gain means that the device will not lase as it cannot overcome the losses, e.g., $g_0 < g_{th}$ when $t_S=60$ nm as shown in Fig. 4. Therefore, careful choice of SiO₂ thickness should be made for the core-shell MCSNLs. The modes are still WGM_{6,2} which are similar to the one shown in Fig. 3.

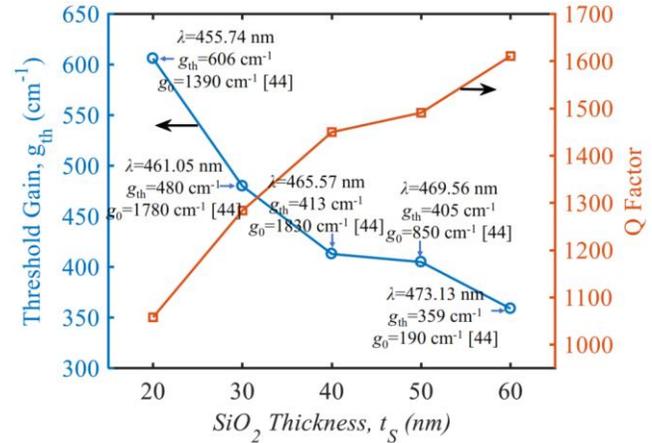


Fig. 4. The influence of SiO₂ thickness on the threshold gain and Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_N=625$ nm, $t_{MQW}=96$ nm and $t_P=80$ nm.

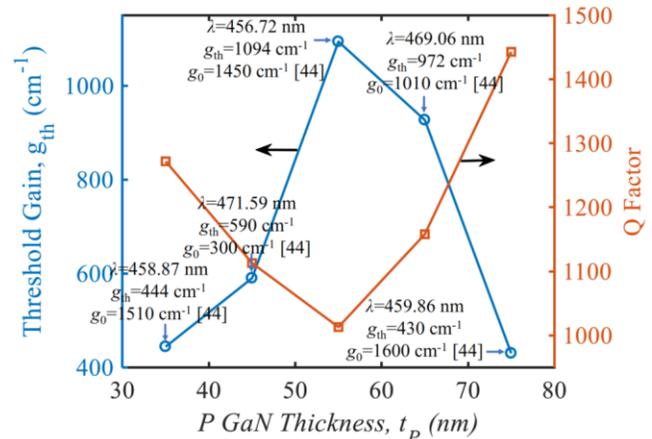


Fig. 5. The influence of P GaN thickness on the threshold gain and Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_N=625$ nm, $t_{MQW}=96$ nm and $t_S=40$ nm.

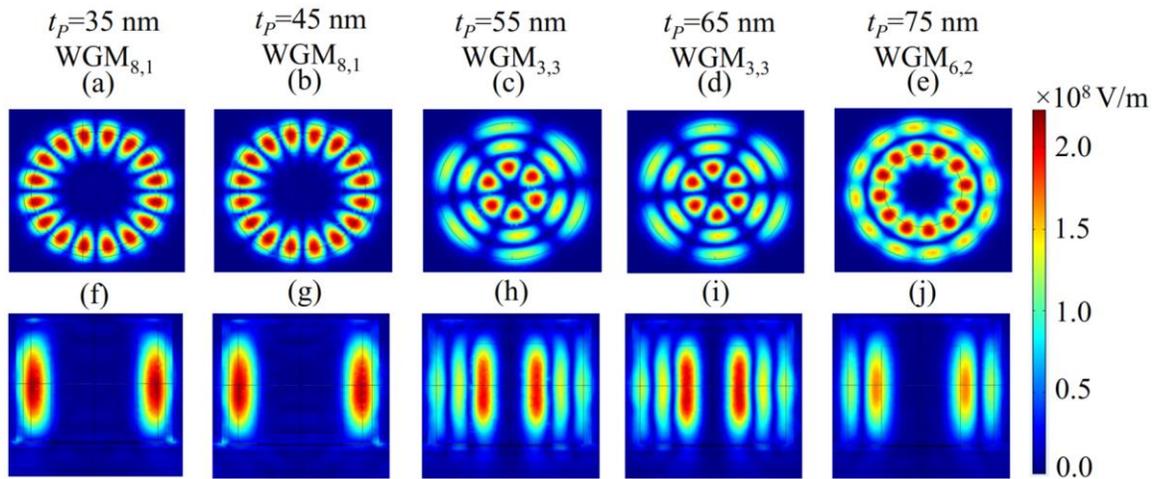


Fig. 6. The corresponding profiles of the modes in Fig. 5.

Attention is finally given to the effect of the P GaN thickness on the threshold gain and the Q factor of the core-shell MCSNL where $r_N=200$ nm, $t_N=650$ nm, $t_{MQW}=96$ nm and $t_S=40$ nm. With increase of t_p thickness, the threshold gain firstly increases to a maximum of 1094 cm^{-1} when $t_p=55$ nm and then decreases to its minimum of 430 cm^{-1} when $t_p=75$ nm as shown in Fig. 5 where the Q factor shows a opposite trend to the threshold gain. The wavelength varies irregularly and thus also does the gain. The biggest difference of gain-loss is 1170 cm^{-1} when $t_p=75$ nm.

The corresponding profiles of the modes in Fig. 5 are shown in Fig. 6. From Fig. 6, it can be seen that the mode profile varies with change of P GaN thickness. When $t_p=35$ and 45 nm, the modes are $\text{WGM}_{8,1}$ and the $t_p=35$ nm has more mode confinement in the MQWs than $t_p=45$ nm, and thus a lower threshold gain. However, when $t_p=55$ and 65 nm, the modes changes to $\text{WGM}_{3,3}$ and most of their electric field intensities are located in the N GaN rather than in the MQWs which leads to a significant increase of the threshold gain. When $t_p=75$ nm, the mode changes to $\text{WGM}_{6,2}$ where most of the electric field intensity of the mode returns to the MQWs. The above effect of P GaN thickness on the modes' behavior is caused by the mode coupling between the co-existing WGM in the cavity with different angular and radial mode numbers. Detailed analysis of mode coupling in the core shell nano-resonator can be found in [68].

IV. ELECTRICAL AND THERMAL SIMULATION RESULTS

The threshold carrier density can be obtained from the steady state form of the laser rate equations. In this situation, the threshold carrier density $N_{th}=N_0+1/(G_N\tau_p)$ where $N_0=9.3\times 10^{19}$ cm^{-3} [69] is the carrier density at transparency, G_N is the gain coefficient and τ_p is the photon life time. $G_N=v_g g$ where v_g is the group velocity and $g=5.8\times 10^{-17}$ cm^2 [69] is the differential gain. $\tau_p=Q\lambda/(2\pi c)$ where Q and λ are extracted from the optical simulation results. c is the speed of light. For the core-shell MCSNL shown in Fig. 3 which has the optimal structure with the lowest threshold gain, the calculated threshold carrier density is $N_{th}=9.7\times 10^{19}$ cm^{-3} . The electrical simulation then shows that the corresponding voltage across and injection

current through the core-shell MCSNL are respectively 3.45 V and 1.5 mA (I_{th}).

Figure 7(a) shows the temperature distribution and heat flux (shown as the red arrows) at threshold. From Fig. 7(a), it can be seen that the majority of the heat generated, largely attributed to the increase of Joule heating, is located around the bottom of P GaN which dissipates through the top coated metal and the substrate. The maximum temperature is 303 K which is only 3 K above the ambient temperature. Generally, increase of temperature will decrease the material gain (which is calculated when temperature is 300 K and the carrier density is 6×10^{19} cm^{-3}). However, the carrier density in this case is 9.7×10^{19} cm^{-3} where the maximum material gain is expected to be above 2500 cm^{-1} when the temperature is 300 K (see Fig. 12 in [44]). Therefore, it is expected the reduction of g_0 due to a 3 K increase of temperature can be sufficiently compensated by increasing the carrier density. In this situation, the material gain is more than six times larger than the loss without significant increase of temperature, thus further confirming the possibility of lasing in the core-shell MCSNL.

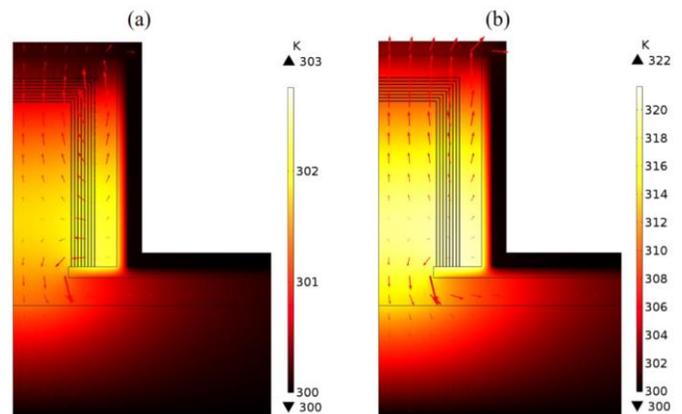


Fig. 7. The temperature distribution and heat flux (red arrows) in the core-shell MCSNL. (a) when the carrier density reaches $N_{th}=9.7\times 10^{19}$ cm^{-3} where voltage=3.45 V, current=1.5 mA, (b) voltage=4.00 V, current=7.6 mA.

With a further increase of injection current to $5.1I_{th}$ (the voltage is 4.00 V), the maximum temperature reaches 322 K and the heat also dissipates through the top coated metal and the

substrate as shown in Fig. 7(b). Such an increased temperature is still in an acceptable range where the gain is not expected to decrease significantly. The good thermal management of the core-shell MCSNL may be attributed to the large thermal conductivities of GaN and large heat capacity of the sapphire substrate. For example, for the MCSNL lasing in the near infrared region which suffers from self-heating problem [32], the thermal conductivity of the active region (InGaAs) is only $16 \text{ Wm}^{-1}\text{K}^{-1}$ [32] which is much less than GaN ($130 \text{ Wm}^{-1}\text{K}^{-1}$ as shown in Table IV). Also, the heat capacity of the InP substrate ($310 \text{ Jkg}^{-1}\text{K}^{-1}$ [70]) is less than that of the sapphire substrate ($880 \text{ Jkg}^{-1}\text{K}^{-1}$ as shown in Table IV).

V. CONCLUSION

In paper, we have designed a metal coated semiconductor nanolaser (SNL) with an GaN/(InGaN/GaN MQWs)/GaN core-shell structure. Numerical results demonstrate that the threshold gain of the SNL is more than four times lower than the material gain calculated in [44] due to the large mode confinement in the active region. Such a low threshold gain indicates the possibility of achieving room temperature (RT) continuous wave (CW) operation of the SNL under electrical injection. This is confirmed by our further simulations which show there is no significant over-heating problem when the SNL is operated well above threshold. The designs of SNL presented in this paper are considered to be helpful for the realization of an electrically pumped RT CW SNL operating in the visible spectral region.

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