Commonality in Liquidity across Options and Stock Futures Markets

Benzennou, Bouchra; ap Gwilym, Owain; Williams, Gwion

Finance Research Letters

13. Mar. 2024

Commonality in Liquidity across Options and Stock Futures Markets

Bouchra Benzennou$^{\pm}$, Owain ap Gwilym and Gwion Williams[1]

This version: 17th December 2018

Abstract

This study investigates the existence of common factors driving liquidity across different markets during a crisis period. The evidence suggests that liquidity across different European options and stock futures markets co-moves. This implies the existence of limits to the potential for liquidity risk management via options and stock futures because both markets experience simultaneous liquidity shocks. These findings are relevant to investors when timing their hedging, speculation, or arbitrage strategies.

Keywords: Liquidity Commonality; Stock Futures; Options

$^{\pm}$ Bouchra Benzennou is a Lecturer in Finance at the School of Economics, Finance, and Accounting, Coventry University, Coventry, United Kingdom. Owain ap Gwilym is a Professor of Finance at Bangor Business School, Bangor University, Bangor, United Kingdom. Gwion Williams is a Lecturer in Finance at Bangor Business School, Bangor University, Bangor, United Kingdom.

[1] Corresponding author, Business School, Bangor University, College Road, Bangor LL57 2DG, United Kingdom. Tel: + 44-1248-382176, email: gwion.williams@bangor.ac.uk.

1. Introduction

Liquidity has been a major aspect of market microstructure research as it is considered a determinant of market behaviour and an indicator of its sound functioning. Early microstructure models seek to explain the idiosyncratic liquidity of individual financial assets, but give little insight on systematic patterns in liquidity. The presence of co-movement in assets' liquidity implies a risk to investors as it represents an undiversifiable portion of liquidity risk. Liquidity co-movement was first investigated by Chordia et al. (2000). They argue that, much like returns, liquidity of single assets might comprise both firm-specific and market components. The latter implies that individual assets' liquidities can be simultaneously affected by market-wide factors, i.e. there exists a commonality in liquidity.

Most studies of liquidity commonality focus on equity markets. Research on other asset classes remains limited (Pu, 2009; Cao and Wei, 2010; Marshall et al., 2013; Verousis et al., 2016). Another underdeveloped yet important research area is commonality in liquidity across different markets (Chordia et al., 2005; Pu, 2009; Mancini et al., 2013; Frino et al., 2014). Specifically, there is no previous study on liquidity commonality across equity options and futures markets. Therefore, this paper makes a well-defined unique contribution and addresses a void in the prior literature. The aim is to investigate the potential presence of commonality in liquidity across European stock futures and options markets during 2008-2010, a period which was characterised by extreme market conditions, when liquidity risk is more likely to materialise.

Taking positions in different markets might enable investors to diversify liquidity risk. In extreme market conditions, there is potentially an increased liquidity risk to investors as margins increase and their positions lose value (Brunnermeier and Pedersen, 2009). For example, Adam-Müller and Panaretou (2009) suggest offsetting such risk related to futures

hedges using options markets. The effectiveness of such hedging would be restricted if liquidity across the two markets co-moves.

Commonality in liquidity across derivatives markets can arise through two possible channels: liquidity provision and liquidity demand. The ability of market makers to provide liquidity depends on their capital and the margins requirements they face. Any information shocks in interest rates, or in the trading volume and price volatility of the underlying assets, will restrict the ability of derivatives market makers to provide liquidity. Under extreme market circumstances, e.g. a financial crisis, liquidity dry-ups in the underlying market will spill over to the futures and options markets. Liquidity providers will incur losses when the market moves against their positions. Traders will face greater difficulty in funding their positions and will face increased margin requirements. Such an environment causes traders to greatly reduce their open positions, thereby leading to a simultaneous decrease in liquidity in both futures and options markets.[2]

Informed trading potentially motivates the demand for futures and options.[3] Information arrival to the underlying market is argued to be the driving factor of simultaneous buying/selling pressures in derivatives markets. This information could lead traders to establish similar perceptions of future returns, volatility, and trading activity in the underlying asset market. This would transmit to their trading demands in futures and options in the same direction. Symmetric shocks to trading activity in derivatives markets can drive liquidity commonality in these markets (see Chordia et al., 2005).

Futures and options markets could experience simultaneous periods of high or low liquidity arising from common liquidity demanders being present in both markets. Assuming the example of basket and institutional trading, several investors are simultaneously

---

[2] Models of supply-side origins of liquidity commonality include: Bernardo and Welch, 2003; Anshuman and Viswanathan, 2005; Brunnermeier and Pedersen, 2009.

[3] Please refer to Black, 1975; Easley et al., 1998; Chakravarty et al., 2004; among others.

buying/selling assets as new information reaches the market. They could seek to enter an offsetting position either in a futures or option contract at the same time, thus leading to simultaneous selling/buying pressures in futures and options markets. Thus, liquidity in both markets would co-move (see Kamara et al., 2008; Karolyi et al., 2012; Lowe, 2014; Koch et al., 2016; Moshirian et al., 2017).

A similar argument can be presented for sentiment-oriented trading. If the price of a given asset is predicted to fall, selling a futures contract or writing a call option on that asset are both potential strategies. When traders share the same sentiment about future price movements, their demand to trade in futures and options markets would take the same direction at the same time, thus inducing liquidity co-movement (Chordia et al., 2000; Bernardo and Welch, 2003; Morris and Shin, 2004). This leads to the second avenue of investigation, which is to question to what extent any revealed liquidity commonality across futures and options markets is driven by common underlying assets. Given the prior discussion in this section, this question has evidently not been addressed in any prior literature.

This paper is organised as follows. Section 2 explains the methodology used to test commonality and describes the data available for this study. Section 3 reports the results, followed by concluding remarks in Section 4.

2. Data and Methodology

2.1. Data selection

High frequency data are obtained from NYSE LIFFE London, Paris, Brussels, and Amsterdam for equity options and futures contracts for January 2008 to December 2010. The global financial crisis period is chosen deliberately, because it was characterised by a tightening in funding liquidity thus potentially revealing strong liquidity commonality (Rösch and Kaserer, 2014). The dataset includes maturity date, strike price (for options), time-stamped volume and price for asks, bids and trades. Our data screening follows the approaches documented in Cao and Wei (2010) and Verousis et al. (2016).

The level of option moneyness is defined as the daily opening price of the underlying equity, S, over the option strike, K, i.e S/K. To avoid pricing issues related to moneyness, deep in-the-money (moneyness greater than 1.1 for calls or less than 0.9 for puts) and deep out-the-money (moneyness less than 0.9 for calls or greater than 1.1 for puts) contracts are dropped. Price data for the underlying assets are from Bloomberg.

Furthermore, contracts whose remaining maturities are either very short (less than 7 days) or very long (more than 90 days) are dropped. Short-maturity contracts are defined as having between 7 and 30 days to maturity; medium-maturity contracts have 31 to 60 days to maturity; long-maturity contracts have 61 to 90 days to maturity. Moreover, contracts with less than 500 observations per year are dropped. Quotes with bid-ask spreads wider than 1.50 are also omitted, following Wei and Zheng (2010).

2.2. Liquidity measures

The following liquidity measures are used: the *relative quoted spread* and the *quoted depth* suggested by Chordia et al. (2000), and *quote slope* suggested by Hasbrouck and Seppi (2001).

The relative spread is one of the most commonly used measures of liquidity. Dividing by the midpoint enables the measure to be comparable across different assets:

$$BAS_{i,t} = \frac{p_{i,t}^A - p_{i,t}^B}{P_{i,t}^M} \qquad (1)$$

Where p_t^A and p_t^B are the ask and bid prices, respectively. The midpoint price is defined as the average of the bid and ask prices: $P_{i,t}^M = \frac{p_{i,t}^A + p_{i,t}^B}{2}$.

Depth measures the ability of the market to process large volumes of trade, with minimum impact on prices. The quoted depth is calculated as the sum of the bid and ask volumes:

$$D_{i,t} = q_{i,t}^A + q_{i,t}^B \qquad (2)$$

Where $q_{i,t}^A$ and $q_{i,t}^B$ are the best ask and the best bid volume in the order book for contract i.

The quote slope, proposed by Hasbrouck and Seppi (2001), is calculated as the spread divided by the log depth. This measure can be illustrated as a linear function whose slope reveals the degree of liquidity. If the quantity of asked or bid contracts increases, or if the buy and sell prices draw closer, the slope decreases, i.e. liquidity improves:

$$QSlope_{i,t} = \frac{p_{i,t}^A - p_{i,t}^B}{\ln(q_{i,t}^A) + \ln(q_{i,t}^B)} \qquad (3)$$

The equally weighted average of each liquidity measure is calculated across each 30-minute interval on a trading day d. There are 16 intervals on each trading day. To neutralise any time-of-the-day effect, the three measures are standardised as follows: let $\tilde{L}_{t,d}^i$ refer to a liquidity measure for a contract i at interval t on day d, μ_t^i and σ_t^i are its mean and standard deviation across intervals t on all days in the sample, respectively (Hasbrouck and Seppi, 2001). Each liquidity measure is standardized as:

$$L_{t,d}^i = \frac{\tilde{L}_{t,d}^i - \mu_t^i}{\sigma_t^i} \qquad (4)$$

2.3. Methodology

According to theoretical predictions, commonality in liquidity is stronger during extreme market conditions. Commonality across futures and options contracts could arise from demand-side factors. Further, it is expected that commonality in liquidity across futures and option contracts with the same underlying assets should be stronger. Two hypotheses are defined:

Hypothesis 1: liquidity commonality across derivative markets – there exist systematic patterns across the liquidities of stock futures and options markets;

Hypothesis 2: common underlying – liquidity exhibits a stronger commonality across stock futures and options written on the same underlying assets.

Commonality tests are conducted using Principal Component Analysis (PCA), following e.g. Connor and Korajczyk (1986), and Korajczyk and Sadka (2008). The principal components are extracted from the observed values of each liquidity measure in futures and options contracts combined. PCA compresses the original liquidity predictors into fewer components which capture the common underlying trend in liquidity of both markets. The emergent components, therefore, record as much information as possible on the variability of the liquidity measure in options and futures. They represent the common underlying factors potentially causing liquidity in both markets to co-move. The strength of these factors in driving commonality in liquidity across markets is given by the R-squared. To this end, each measure is regressed on the extracted components as follows:

$$L_{t,d}^i = \beta^i F_{t,d} + \varepsilon_{t,d}^i \qquad (5)$$

7

Where $F_{t,d}$ is the vector of extracted common factors in interval t on a trading day d. The cross-sectional average R^2 of the above regression indicates whether there is commonality in the liquidity measure in question. The higher is the R^2, the stronger the commonality.

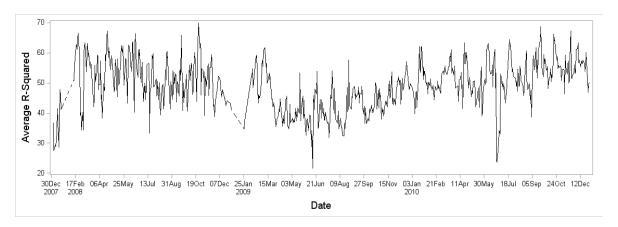## 3. Results

3.1. All contracts

Figure 1: Daily Commonality across SSF and Options Markets
This figure displays the time series dynamics of commonality in the bid-ask spread across SSF and options markets. The level of commonality is quantified by the daily cross-sectional average of R^2 value, the goodness of fit of the following regression model:
$$BAS_{t,d}^i = \beta^i F_{t,d} + \varepsilon_{t,d}^i$$
Where $BAS_{t,d}^i$ is the bid-ask spread of contact i at interval t on day d and $F_{t,d}$ is the vector of extracted common factors in interval t on a trading day d.

Figure 1 displays the daily dynamics of R-squared in the bid-ask spread across SSF and options markets. The figure shows that the level of commonality is high throughout the time series and varies by approximately 50%, on average. This is confirmed by the PCA results reported in Table 1, which includes the eigenvalues and cumulative contributions of each component, and the cross-sectional average R-squared. Panel A includes all contract maturities; Panels B, C, and D represent short-, medium-, long-maturity contracts, respectively.

Factor	Spread			Depth			Qslope		
	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)
PANEL A: All contract maturities (N=1034)									
1	155.37	15.71	13.86	85.84	10.28	11.65	234.89	23.92	20.02
2	61.07	21.88	20.68	64.18	17.97	20.79	129.11	37.07	35.52
3	40.48	25.98	26.49	59.23	25.06	27.03	48.84	42.04	42.00
PANEL B: Short-maturity contracts (N=347)									
1	62.84	19.16	17.41	40.70	15.36	14.38	102.41	29.86	25.77
2	23.71	26.38	26.15	22.72	23.93	23.19	58.98	47.05	45.98
3	16.45	31.40	31.98	18.71	30.99	30.22	15.42	51.55	50.50
PANEL C: Medium-maturity contracts (N=353)									
1	51.01	15.99	14.58	51.91	15.40	13.17	92.72	26.64	21.00
2	20.51	22.42	23.69	28.44	23.84	22.06	55.02	42.45	41.58
3	15.96	27.42	28.63	25.50	31.41	29.77	14.51	46.62	45.79
PANEL D: Long-maturity contracts (N=334)									
1	60.43	14.42	15.41	45.23	14.64	12.88	77.45	24.36	20.19
2	31.17	21.86	23.56	31.78	24.92	25.22	39.66	36.83	36.02
3	22.85	27.31	28.78	27.48	33.82	34.45	19.16	42.85	42.66

Table 1: Principal Component Analysis of Relative Spread, Depth, and Qslope across Stock Futures and Options Markets

The table reports the eigenvalues and the cumulative contribution of the first three components extracted from the principal component analysis, as well as the cross-sectional average R-squared for the time-series regression of each contract's liquidity measure (including stock futures and options) on the first, the first two, and the first three components, as specified in:

$$L_{t,d}^i = \beta^i F_{t,d} + \varepsilon_{t,d}^i$$

Where $L_{t,d}^i$ is the liquidity measure standardised using its mean and standard deviation in interval t across all days in the sample.

Table 1 reveals ample evidence of commonality in liquidity across stock futures and options markets. The strongest commonality occurs in Qslope. In Panel A, the extracted components account for 42% of the total variance of Qslope for both futures and option contracts. Commonality is at similar levels for both relative spread and depth, with the total variances explained by the components being 26% and 25%, respectively. This implies that there are underlying factors driving from 25% to 42% of liquidity of stock futures and options

simultaneously. Commonality in Qslope and spreads is strongest for short-maturity contracts, while long-maturity contracts exhibit the highest level of systematic patterns in liquidity measured by depth. This implies that short-maturity contracts are more sensitive to changes in markets' spreads, while long-maturity contracts are more sensitive to changes in markets' depth. Short hedgers aiming to sell an asset or speculators aiming to achieve short-term profits would take positions in short-maturity contracts. During extreme market conditions, the costs of trading and the risk associated with such positions increase, thus overall spreads widen. Long-maturity contracts are selected by institutional investors willing to enter long hedge positions, particularly when prices are volatile. During periods of intense institutional trading, markets' ability to sustain large orders decreases.

3.2. Common-underlying contracts

Further tests investigate whether contracts written on the same asset exhibit stronger commonality in liquidity. After excluding contracts with different underlying assets, the PCA is used to extract the first most meaningful components explaining a large proportion of variation in liquidity measured by relative spread, depth, and Qslope. Table 2 reports the eigenvalues and cumulative contributions of each component, and the cross-sectional average R-squared.

The results presented in Table 2 confirm the presence of strong co-movement in liquidity across stock futures and options markets. Consistent with Table 1, the strongest commonality occurs in Qslope. Commonality remains evident when liquidity is measured by depth and relative spread. As in the previous analysis, the results reveal that commonality in Qslope and spreads is stronger for short-maturity contracts, whereas it is stronger for long-maturity contracts' depth.

Factor	Spread			Depth			Qslope		
	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)	Eigen-value	Cumulative Explained Variance (%)	R-squared (%)
PANEL A: All contract maturities (N=357)									
1	78.14	23.75	21.68	40.40	13.25	13.00	130.65	37.12	33.45
2	22.79	30.68	29.23	35.79	24.98	23.77	68.13	56.47	55.21
3	15.06	35.25	35.74	20.55	31.72	31.04	12.60	60.05	58.93
PANEL B: Short-maturity contracts (N=119)									
1	32.40	28.42	25.77	11.14	12.66	11.95	45.82	39.84	36.78
2	8.97	36.29	34.72	8.05	21.81	19.44	24.01	60.72	58.94
3	5.95	41.51	41.64	7.06	29.84	30.38	4.53	64.66	63.12
PANEL C: Medium-maturity contracts (N=121)									
1	27.39	24.46	22.54	15.82	14.25	12.23	45.71	37.78	34.27
2	8.69	32.22	31.33	13.88	26.76	24.01	25.27	58.67	57.36
3	6.01	37.59	37.95	9.15	35.01	34.20	4.74	62.59	61.36
PANEL D: Long-maturity contracts (N=117)									
1	24.34	22.53	22.71	15.83	16.67	14.15	33.66	33.00	24.92
2	9.02	30.89	30.59	12.92	30.27	28.14	17.14	49.81	48.11
3	6.09	36.53	36.95	7.52	38.18	39.77	5.46	55.17	54.33

Table 2: Principal Component Analysis of Relative Spread, Depth, and Qslope across Stock Futures and Options Contracts with Common Underlying Assets

The table reports the eigenvalues and the cumulative contribution of the first three components extracted from the principal component analysis, as well as the cross-sectional average R-squared for the time-series regression of each contract's liquidity measure (including only stock futures and options written on the same underlying asset) on the first, the first two, and the first three components, as specified in:

$$L_{t,d}^i = \beta^i F_{t,d} + \varepsilon_{t,d}^i$$

Where $L_{t,d}^i$ is the liquidity measure standardised using its mean and standard deviation in interval t across all days in the sample.

Decomposing components using contracts written on the same underlying assets demonstrates increased explanatory power and their contribution in total variance of all liquidity measures. For instance, the cumulative explained variance of the QSlope is nearly 60% in contracts written on the same underlying assets, compared to 42% for the full set of assets. The emergent components for spread explain approximately 26% of the total variance

in the full sample, whereas they account for up to 35% of the total variance in contracts with common underlying assets. Similar comparisons are observed for depth and QSlope.

4. Discussion and Conclusions

This study reveals the presence of common factors affecting liquidity in stock futures and options simultaneously during a crisis period. The principal component analysis reveals first-time evidence on co-movement in liquidity across the two derivative markets, potentially owing to common trading behaviour, institutional ownership, or investor sentiment. Systematic patterns in liquidity can also emerge from the underlying asset's characteristics and trading, as proposed by Cao and Wei (2010) who show that the degree of commonality in options is related to the size and volatility of the underlying stock. In further tests of commonality across stock futures and options written on the same underlying asset, our results reveal a greater extent of liquidity commonality. Overall, commonality across stock futures and options, whether these share the same underlying asset or not, remains high enough to conclude that a liquidity shock in stock futures is accompanied by a similar shock in the equity options market, and vice versa. These findings suggest that market participants need to be wary when constructing their hedging, speculation, and arbitrage strategies during periods of simultaneous low liquidity in both derivative markets. The results imply that investors are not able to diversify their liquidity needs by opening positions in different derivative markets, as liquidity shocks occur simultaneously in both markets, although geographically and contractually distinct. During liquidity dry-ups, transaction costs increase and market depth decreases concurrently in both markets, i.e. offsetting a position across markets becomes more costly, the ability of investors to maintain their margin accounts is diminished and their exposure to liquidity risk is increased. The co-movement of liquidity in both markets suggests that cross-market strategies to diversify systematic liquidity risk might not be particularly successful.

REFERENCES

Adam-Müller, A. & Panaretou, A. (2009) Risk Management with Options and Futures under Liquidity Risk. Journal of Futures Markets, 29, 297–318.

Anshuman, R. & Viswanathan, S. (2005). Costly Collateral and Liquidity. Working paper, Duke University.

Bernardo, A. & Welch, I. (2003). Liquidity and Financial Market Runs. Quarterly Journal of Economics, 119, 135–158.

Black, F. (1975). Fact and Fantasy in Use of Options. Financial Analysts Journal, 31, 36–41.

Brunnermeier, M. & Pedersen, L. (2009). Market Liquidity and Funding Liquidity. Review of Financial Studies, 22, 2201–2238.

Cao, M. & Wei, J. (2010). Option Market Liquidity: Commonality and Other Characteristics. Journal of Financial Markets, 13, 20–48.

Chakravarty, S., Gulen, H., & Mayhew, S. (2004). Informed Trading in Stock and Option Markets. Journal of Finance, 59, 1235–1257.

Chordia, T., Roll, R., & Subrahmanyam, A. (2000). Commonality in Liquidity. Journal of Financial Economics, 56, 3–28.

Chordia, T., Sarkar, A., & Subrahmanyam, A. (2005). An Empirical Analysis of Stock and Bond Market Liquidity. Review of Financial Studies, 18, 85–129.

Connor, G. & Korajczyk, R (1986). Estimating Pervasive Economic Factors with Missing Observations. Working Paper, Northwestern University.

Easley, D., O'Hara, M., & Srinivas. P. (1998). Option Volume and Stock Prices: Evidence on where Informed Traders Trade. Journal of Finance, 53, 431–465.

Frino, A., Mollica, V., & Zhou, Z. (2014). Commonality in Liquidity across International Borders: Evidence from Futures Markets. Journal of Futures Markets, 34, 807–818.

Hasbrouck, J. & Seppi, D. (2001). Common Factors in Prices, Order Flows, and Liquidity. Journal of Financial Economics, 59, 383–411.

Kamara, A., Lou, X. & Sadka, R. (2008). The Divergence of Liquidity Commonality in the Cross-Section of Stocks. Journal of Financial Economics, 89, 444–466.

Karolyi, G., Lee, K., & van Dijk, M. (2012). Understanding Commonality in Liquidity around the World. Journal of Financial Economics 105, 82–112.

Koch, A., Ruenzi, S., & Starks, L. (2016). Commonality in Liquidity: A Demand-Side Explanation. Review of Financial Studies, 29, 1943–1974.

Korajczyk, R. & Sadka, R. (2008). Pricing the Commonality across Alternative Measures of Liquidity. Journal of Financial Economics, 87, 45–72.

Lowe, A. (2014). The Demand-side Explanation for Commonality in Liquidity: The Role of Institutional Ownership in the Taiwan Stock Exchange. Pacific-Basin Finance Journal, 29, 59–85.

Mancini, L., Ranaldo, A., & Wrampelmeyer, J. (2013). Liquidity in the Foreign Exchange Market: Measurement, Commonality, and Risk Premiums. Journal of Finance, 68, 1805–1841.

Marshall, B., Nguyen, N., & Visaltanachoti, N. (2013). Liquidity Commonality in Commodities. Journal of Banking & Finance, 37, 11–20.

Morris, S. & Shin, H. (2004). Liquidity Black Holes. Review of Finance, 8, 1–18.

Moshirian, F., Qian, X., Wee, C., & Zhang, B. (2017). The Determinants and Pricing of Liquidity Commonality around the World. Journal of Financial Markets, 33, 22–41.

Pu, X. (2009). Liquidity Commonality across Bond and CDS Markets. Journal of Fixed Income, 19, 26–39.

Rösch, C. & Kaserer, C. (2014). Reprint of: Market Liquidity in the Financial Crisis: The Role of Liquidity Commonality and Flight-To-Quality. Journal of Banking and Finance, 45, 152–170.

Verousis, T, ap Gwilym, O. & Voukelatos, N. (2016). Commonality in Equity Options Liquidity: Evidence from European Markets. European Journal of Finance, 22 (12), 1204–1223.

Wei, J. & Zheng, J. (2010), Trading Activity and Bid-Ask Spreads of Individual Equity Options. Journal of Banking and Finance, 34, 2897–2916.